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PROBLEMS AND SOLUTIONS.

EDITED BY B. F. FINKEL AND R. P. BAKER.

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PROBLEMS FOR SOLUTION.

ALGEBRA.

450. Proposed by J. E. ROWE, Pennsylvania State College.

If the four roots of the quartic equation $A \equiv a_0x^4 + 4a_1x^3 + 6a_2x^2 + 4a_3x + a_4 = 0$, are so related that $B \equiv a_0a_4 - 4a_1a_3 + 3a_2^2 = 0$, show by elementary algebra that two roots of A are real and two imaginary. Show also by means of elementary algebra that A cannot have two equal roots without having three, if the condition $B = 0$ is satisfied.

451. Proposed by H. S. UHLER, Yale University.

Prove that

$$\frac{\sin x}{x} = \cos \frac{x}{2} \cos \frac{x}{2^2} \cos \frac{x}{2^3} \cos \frac{x}{2^4} \cdots$$

GEOMETRY.

481. Proposed by PAUL CAPRON, U. S. Naval Academy.

Show that the locus of the intersection of a pair of perpendicular normals to a parabola $y^2 = 4px$ is the parabola $y^2 = p(x - 3p)$.

482. Proposed by ROBERT G. THOMAS, The Citadel, Charleston, S. C.

In laying out a kite-shaped mile race-track, composed of a circular arc and two intersecting tangents at the ends of the arc, determine the angle at the center of the arc (α) when the length of the arc equals the sum of the two tangents, and (b) when the arc is equal to the length of each tangent.

CALCULUS.

402. Proposed by C. N. SCHMALL, New York City.

If (x, y) be a double point on the curve $u \equiv f(x, y) = 0$, show that (1) the two branches of the curve will cut orthogonally if

$$\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = 0;$$

and (2) if this point be made the origin, then the equation of the tangents to the branches will be

$$(y'^2 - x'^2) \frac{\partial^2 u}{\partial x^2} + 2x'y' \frac{\partial^2 u}{\partial x \partial y} = 0,$$

where (x', y') are the current coördinates of points on the tangents.

NOTE.—In an early issue, we will publish all the unsolved problems in Number Theory proposed from January, 1913, to December, 1915. EDITORS.

SOLUTIONS OF PROBLEMS.

ALGEBRA.

439. Proposed by A. M. KENYON, Purdue University.

If k, n are natural numbers, $n > 2k$, show that

$$\frac{2^k}{[k]} \frac{I\left(\frac{n+1}{2}\right)}{\sum_{i=0}^k \frac{1}{[2i+1][n-k-2i]}} = \frac{2^n}{[n+1]} \sum_{i=0}^k \binom{n-i}{n-k},$$

where $I(n/2)$ denotes the integral part of $n/2$ and $\binom{n}{k}$ is the coefficient of x^k in $(1+x)^n$.